

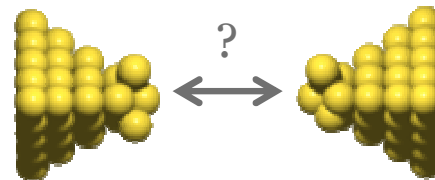


Absolute distances in nano-sized tunnel junctions

Group meeting

May 12, 2010

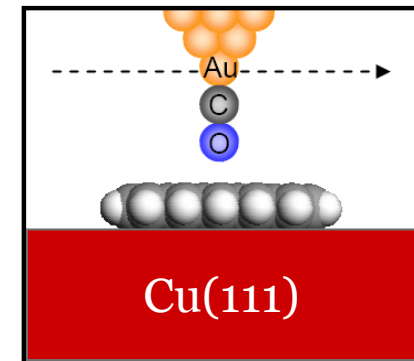
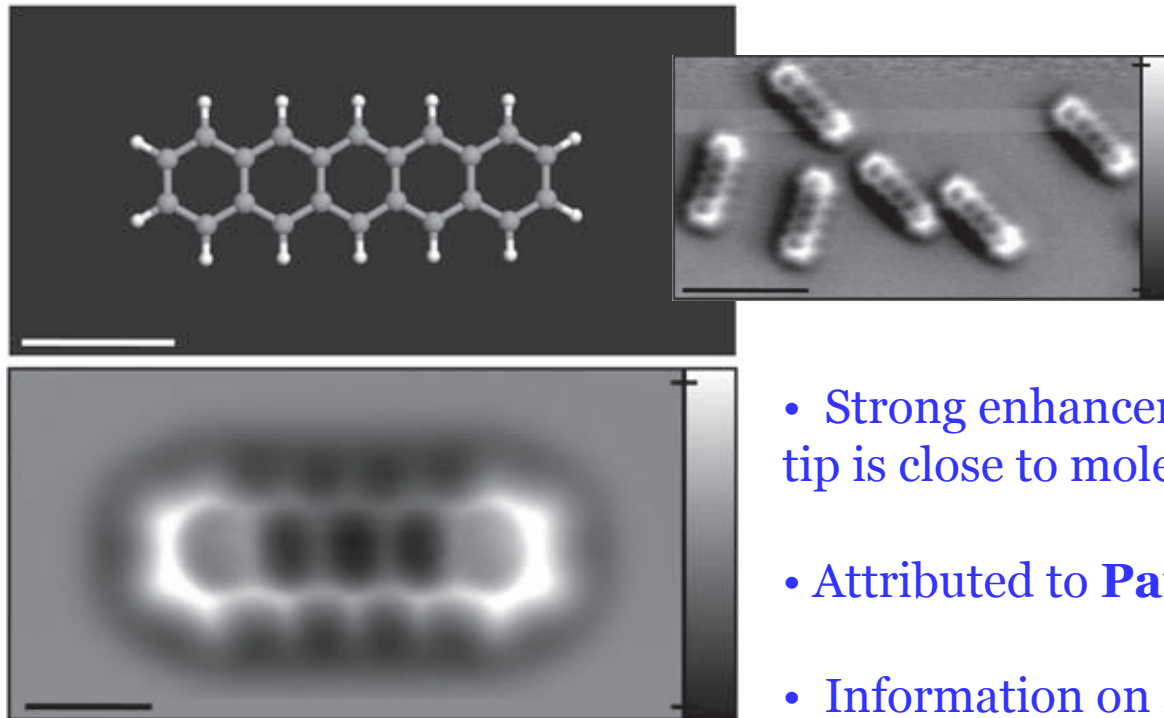
Marius Trouwborst





High resolution imaging

AFM image of Pentacene on Cu(111) at 5 K.



- Strong enhancement in resolution when tip is close to molecule ($1\text{\AA} < d < 2\text{\AA}$).
- Attributed to **Pauli Repulsive forces**.
- Information on absolute distance is crucial



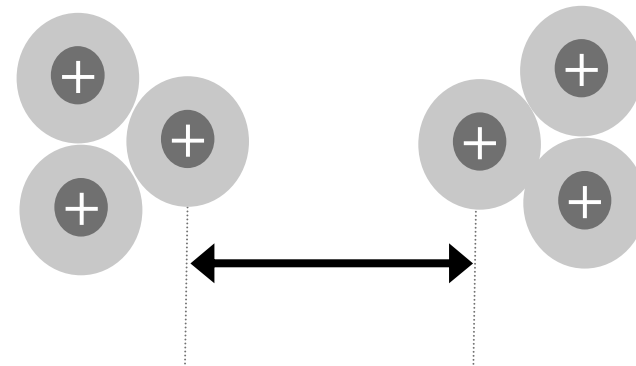
Overview: effects on electrode separation

Various forces involved:

- Electrostatic forces
- Van der Waals forces
- Metallic forces
- Pauli Repulsive forces

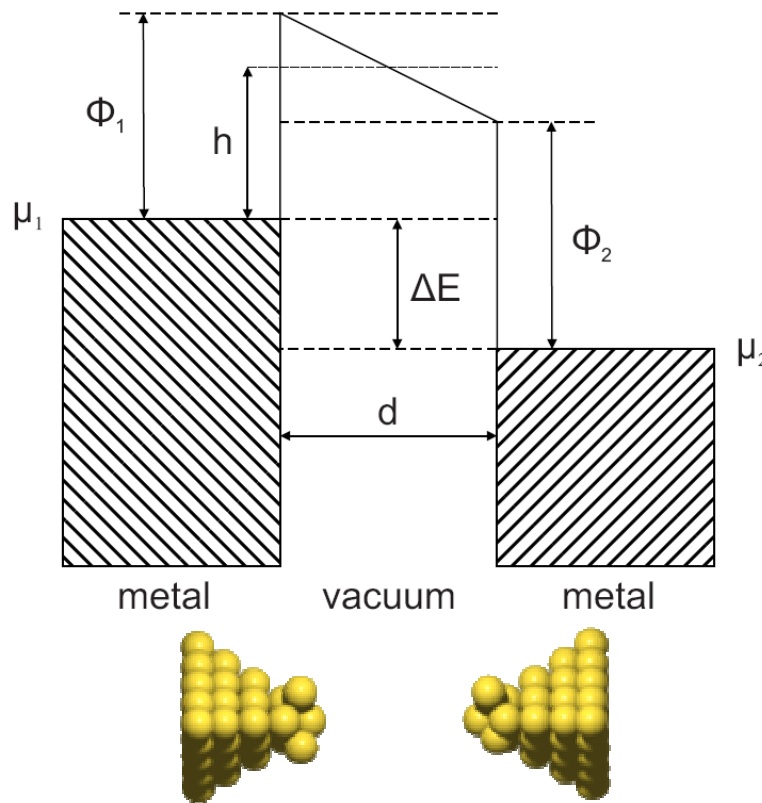
Other effects influencing conductance and/or electrode separation:

- Thermal effects (expansion)
- Image potential





Simple square barrier model



$$G = \frac{2e^2}{h} T = \frac{2e^2}{h} e^{-2\kappa d}$$

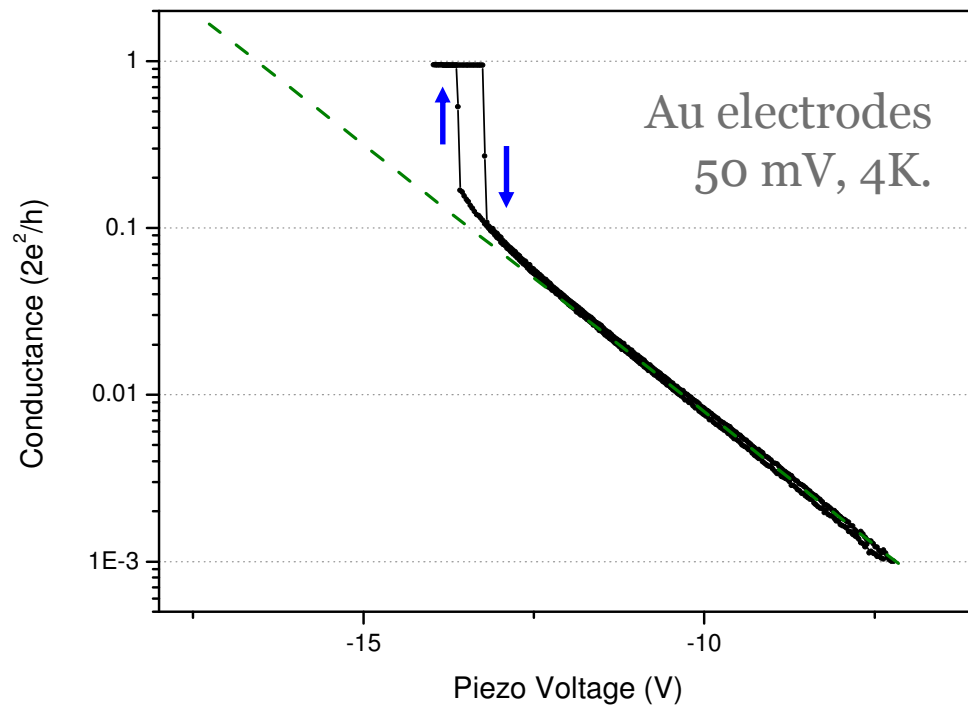
$$\kappa = \sqrt{2m\phi}/\hbar.$$

For gold (5.4 eV):

$$\Delta \text{Log}G/\Delta D \approx -1 \text{ \AA}^{-1}$$



Conductance in tunneling regime



For $G < 0.05 G_0$, tunnel conductance decreases exponentially with distance

$$G = \frac{2e^2}{h} T = \frac{2e^2}{h} e^{-2\kappa d}$$

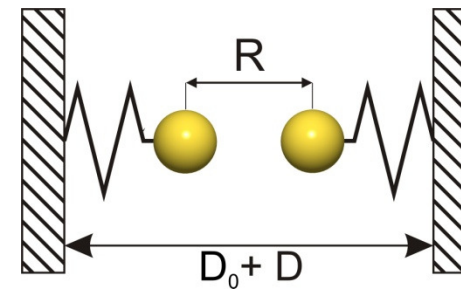
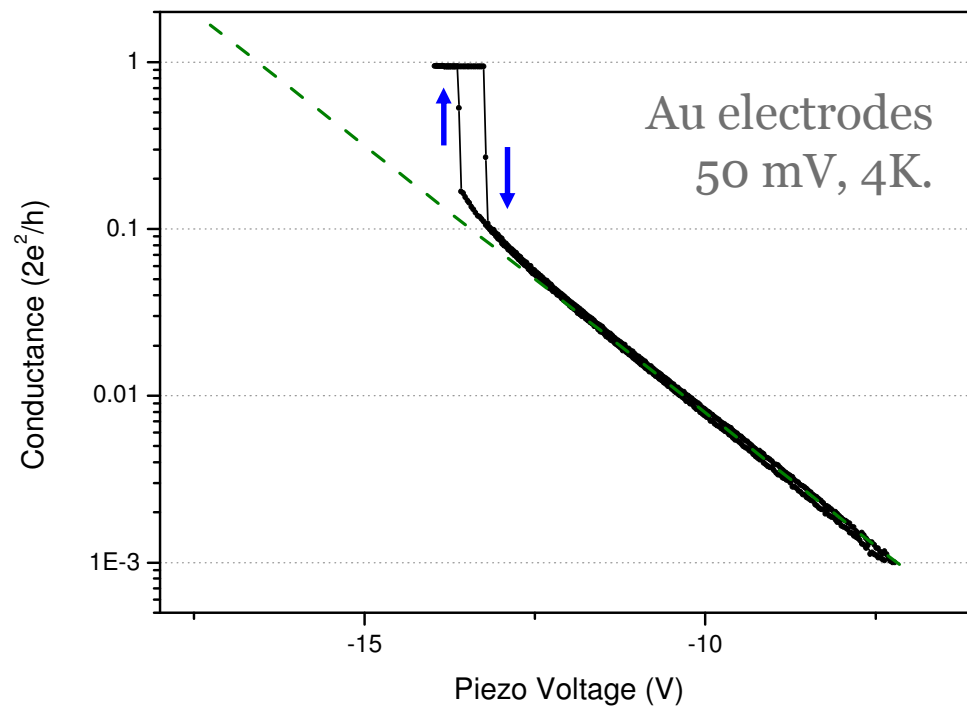
$$\kappa = \sqrt{2m\phi}/\hbar.$$

For gold (5.4 eV):

$$\Delta \text{Log}G / \Delta D \approx -1 \text{ \AA}^{-1}$$

At $\sim 0.1 G_0$, deviation from exponential tunneling due to metallic interaction

Metallic binding forces

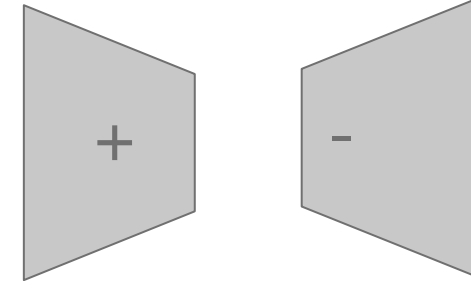


For $G < 0.1 G_0$, jump to contact
due to atomic binding forces

Reduced electrode distance
due to attractive forces



Electrostatic interactions



$$\left. \begin{array}{l} C = \epsilon A/d \\ U = C V^2/A \end{array} \right\} F_{\text{electrostatic}} = \epsilon A V^2/d \approx 0.05 \text{ nN}$$

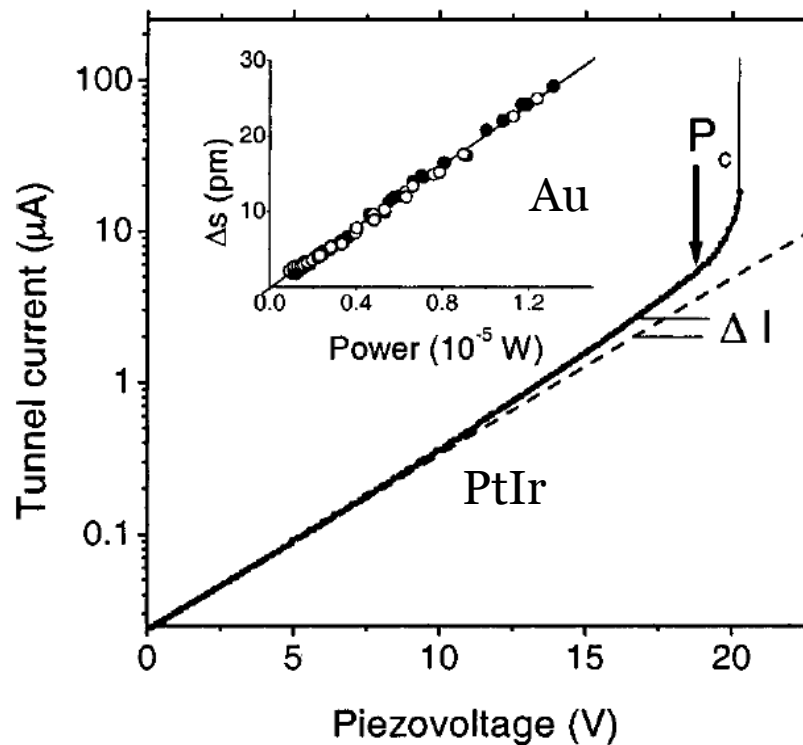
Area $\approx 1 \times 1 \text{ nm}$

Bias voltage $\approx 1 \text{ V}$ Distance $\approx 2 \text{ \AA}$

Rough estimation: junction with spring constant $\approx 1 \text{ N/m}$ could result in 0.5 \AA smaller electrode gap (at 1 V , 2 \AA).



Heating / Thermal expansion

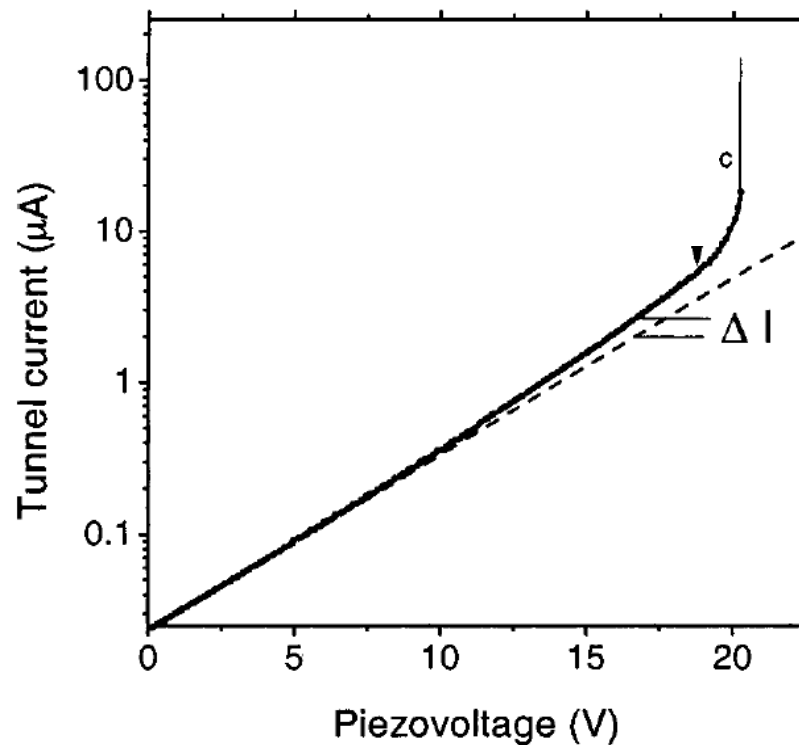


$$P = V^2/R$$
$$2V, 1 \text{ M}\Omega = 4 \mu\text{W}$$

Power dissipation of $4 \mu\text{W}$
could result in ~ 0.1 Ångstrom
smaller electrode gap



Thermal expansion & electrostatic forces



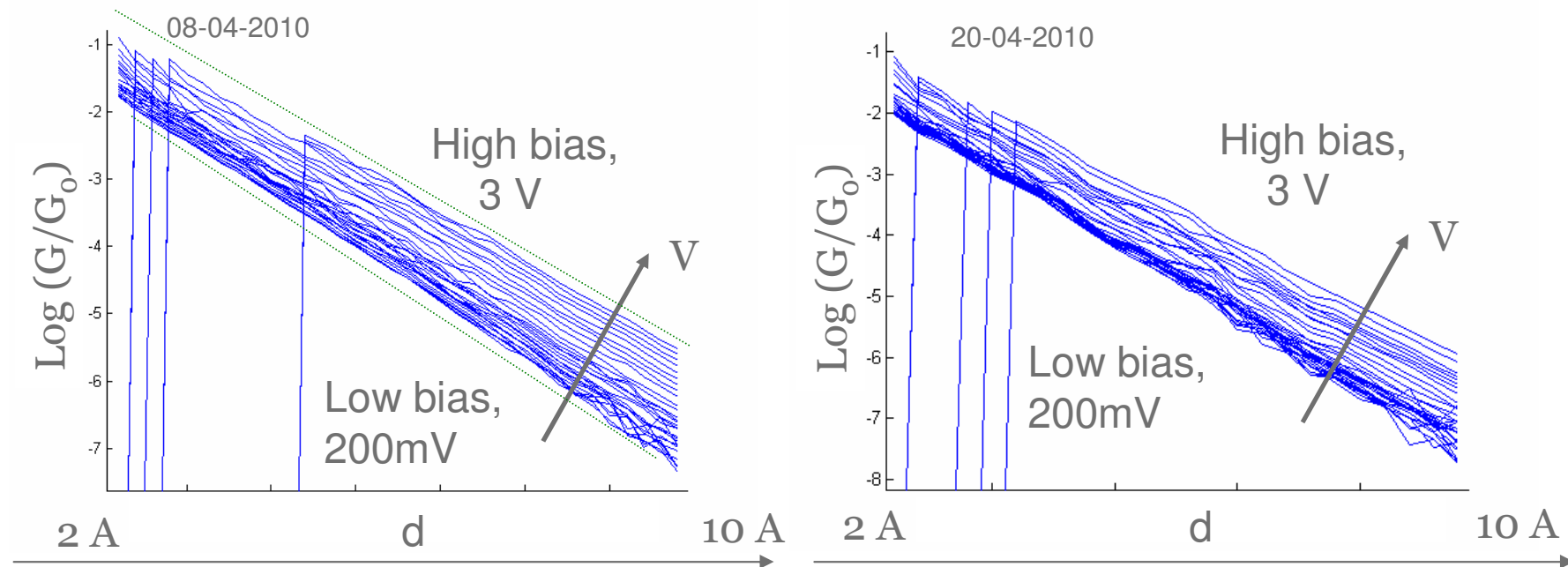
Both effects would decrease the electrode separation.

This would result in deviation in dI/dV from exponential behavior.

Repeat measurements at higher bias voltages.



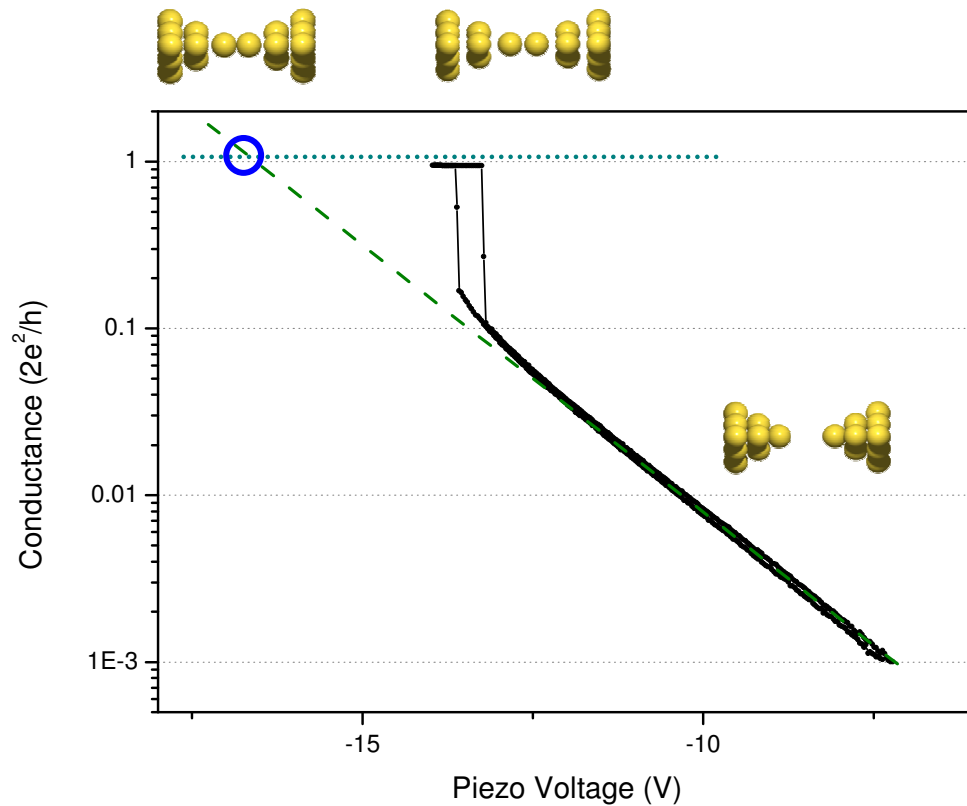
dI/dV as a function of d



- dI/dV measurements for different bias voltages (steps of 200 mV).
- The overall slope of $dI/dV(d)$ decreases with increasing bias voltage $\bar{\varphi} = (\varphi - eV/2)$.
- **No systematic deviations from exponential behavior for larger biases (up to ~ 2 V, $0.01 G_0$).**



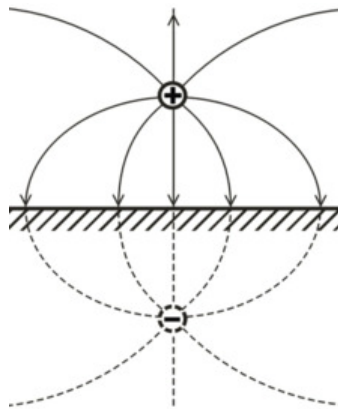
Absolute electrode separation



Zero electrode separation by extrapolating to $1 G_0$?

Take into account barrier lowering by *image charges*!

Image charges & real barrier



- Image charges strongly reduce potential barrier.
- **The reduced barrier, however, has never been directly observed in tunnel junctions:**
 - 1) Only second order effect on tunnel slope.
 - 2) Effect cancels out by metallic adhesion.

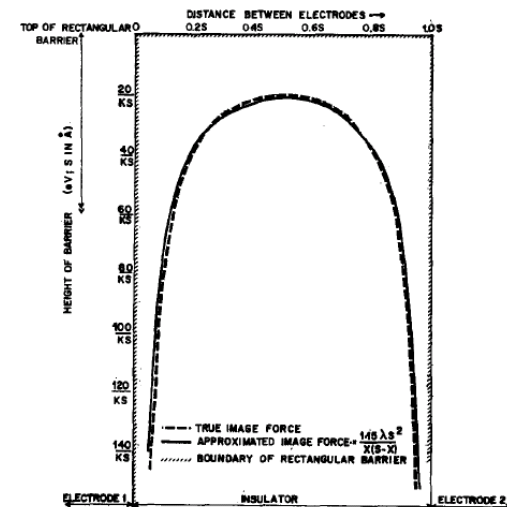




Image charges & real barrier

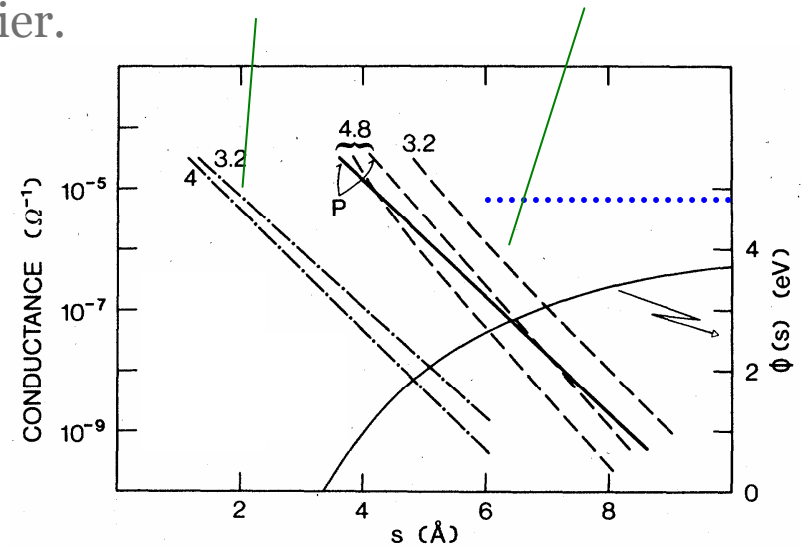
Image charges strongly reduce potential barrier.

Assume: $\phi(d) = \phi_0 - \frac{\alpha}{d}$ 10 eVÅ

$$I \propto \exp[-2d\sqrt{\phi(d)}]$$

$$\frac{d(\ln I)}{ds} = 2\phi_0^{1/2} \left[1 + \frac{\alpha^2}{8\phi_0^2 d^2} + O\left(\frac{1}{d^3}\right) \right] (1 + \beta)$$

Without Image forces With Image forces

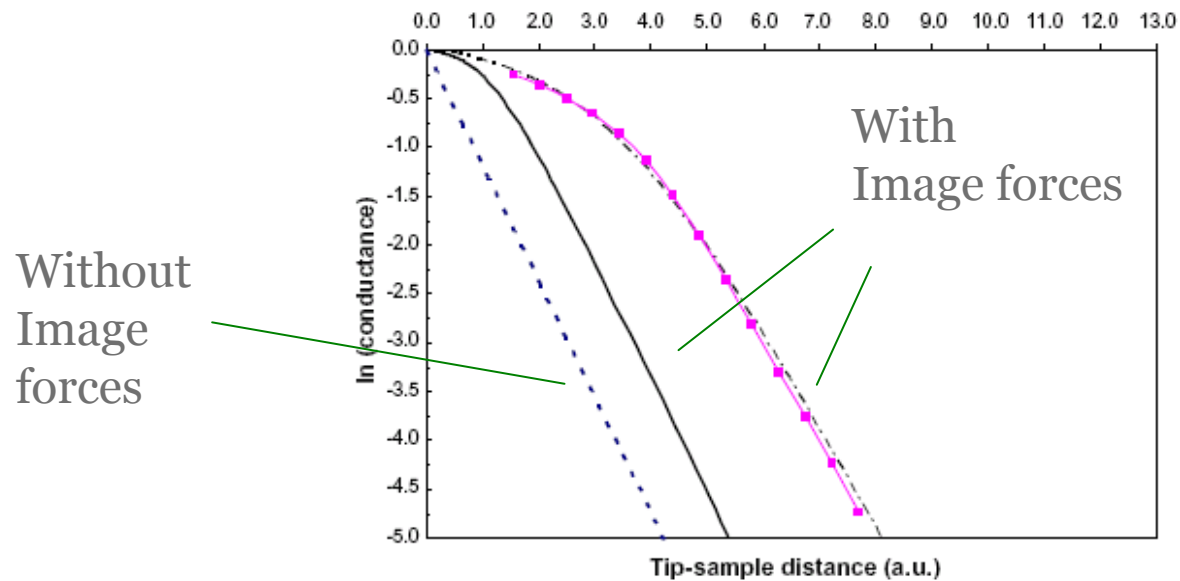


The tunnel slope (dI/dV(d)) hardly effected due to **second order** correction.

The absolute conductance, however, increases dramatically.



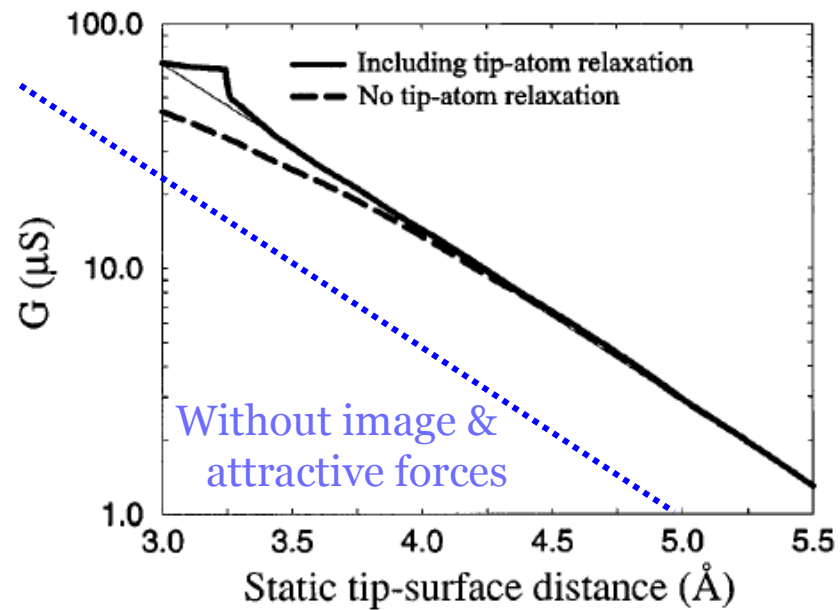
Image charges & real barrier



Change in tunnel slope only at small electrode gaps.
The absolute conductance increases dramatically ($>10^*$).
Strongly depends on exact model.



Image charges & real barrier



Change in tunnel slope cancels out by attractive metallic forces



Image charges & real barrier

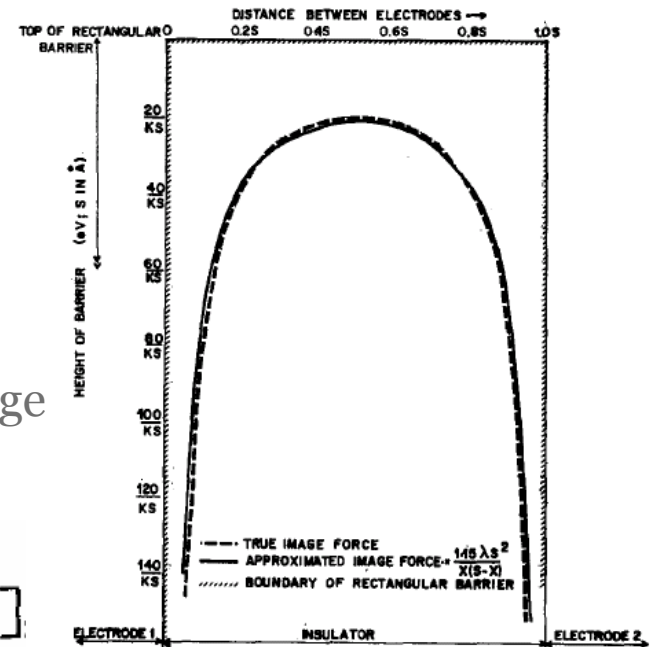
More complete description of image barrier includes influence of bias voltage

Square barrier height

High bias voltage correction

zero bias voltage correction

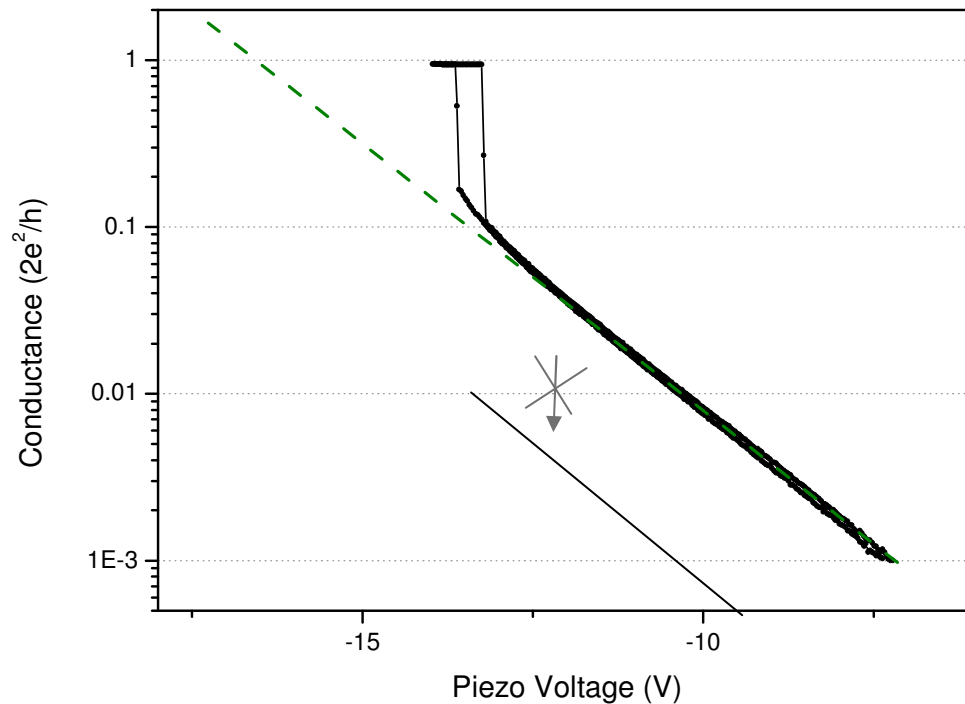
$$\varphi_I = \varphi_0 - (V/2s)(s_1 + s_2) - [5.75/K(s_2 - s_1)] \ln[s_2(s - s_1)/s_1(s - s_2)]$$



For a more accurate description, the shape of the electrodes should be included



Image charges & real barrier



Note: the jump to contact can not occur at much larger electrode Separations.



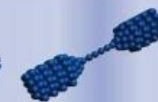
Conclusions

- › For our junction geometry, heating or electric field does not change the electrode separation for voltages up to 2 V over 1 M Ω tunnel barrier.
- › The image potential is expected to have a large influence on the conductance (increase up to 3 orders of magnitude). Hence, there is a large uncertainty about the absolute electrode separation.

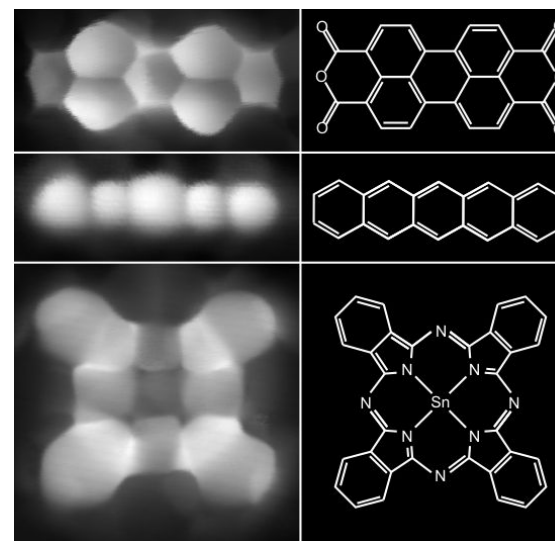
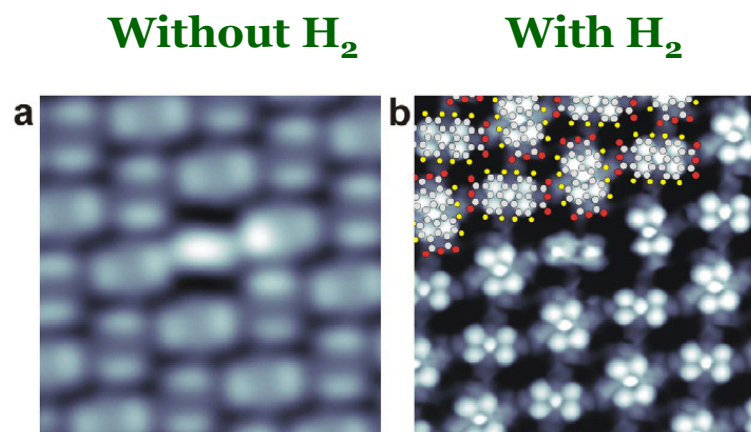


Universiteit Leiden

Appendix



Present work: Enhanced STM resolution with H₂

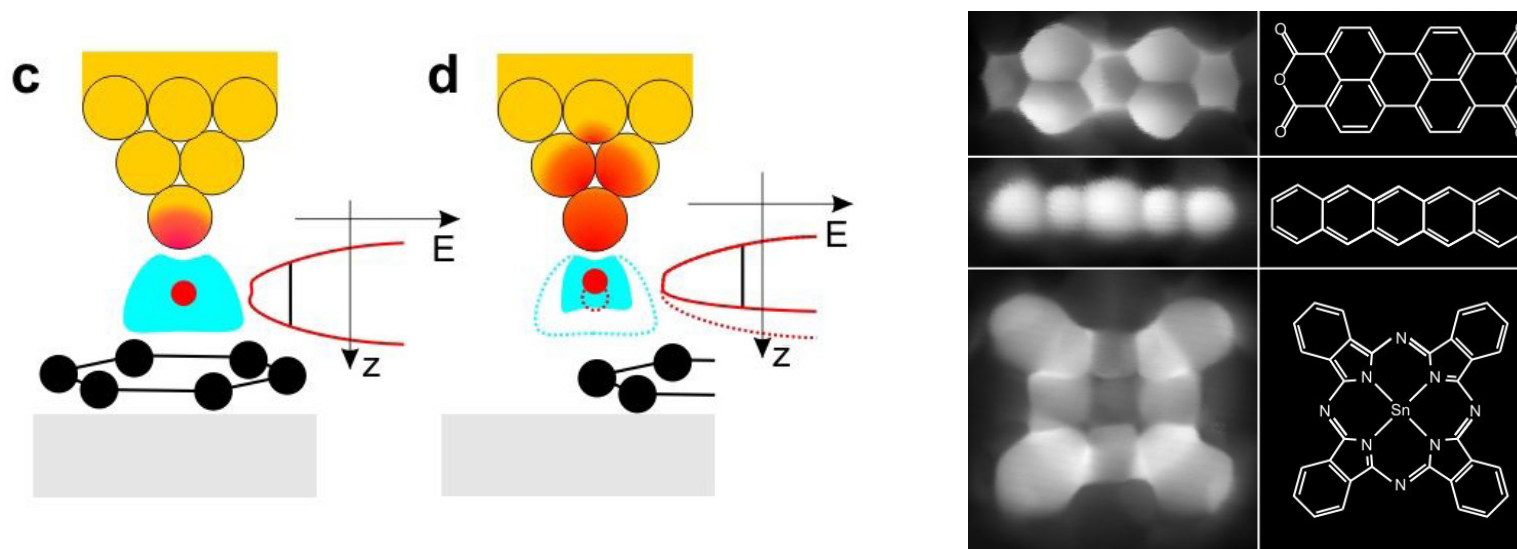


- STM resolution highly enhanced in hydrogen atmosphere.
- Chemical structure resolved.

 Ruslan Temirov, Stefan Tautz *et al*, New Journal of Physics **10** (2008) 053012
[arXiv:0910.5825](https://arxiv.org/abs/0910.5825)



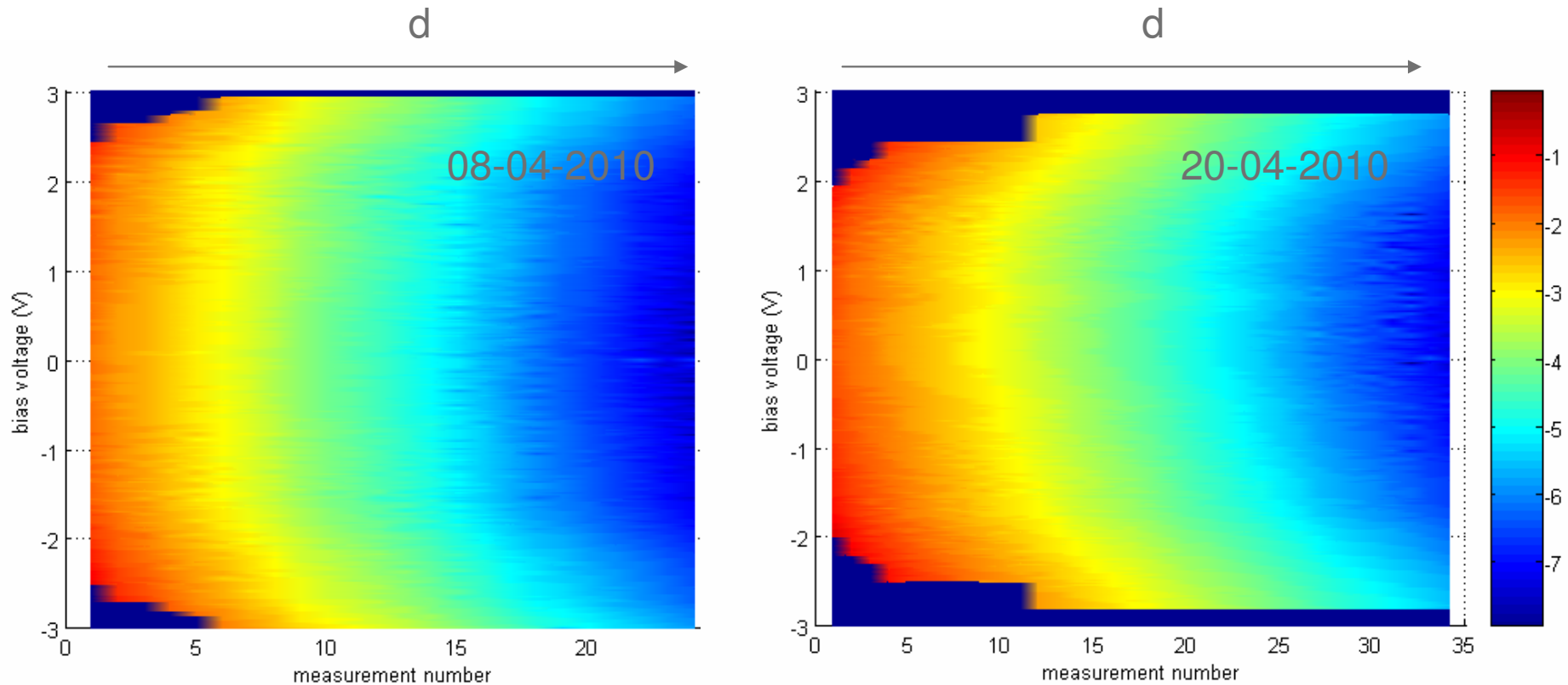
Present work: Enhanced STM resolution with H₂



- Chemical structure resolved
- Possibly due to “Pauli repulsion”

Similar effect in ⁴He environment?

Ruslan Temirov, Stefan Tautz *et al*, New Journal of Physics **10** (2008) 053012
[arXiv:0910.5825](https://arxiv.org/abs/0910.5825)

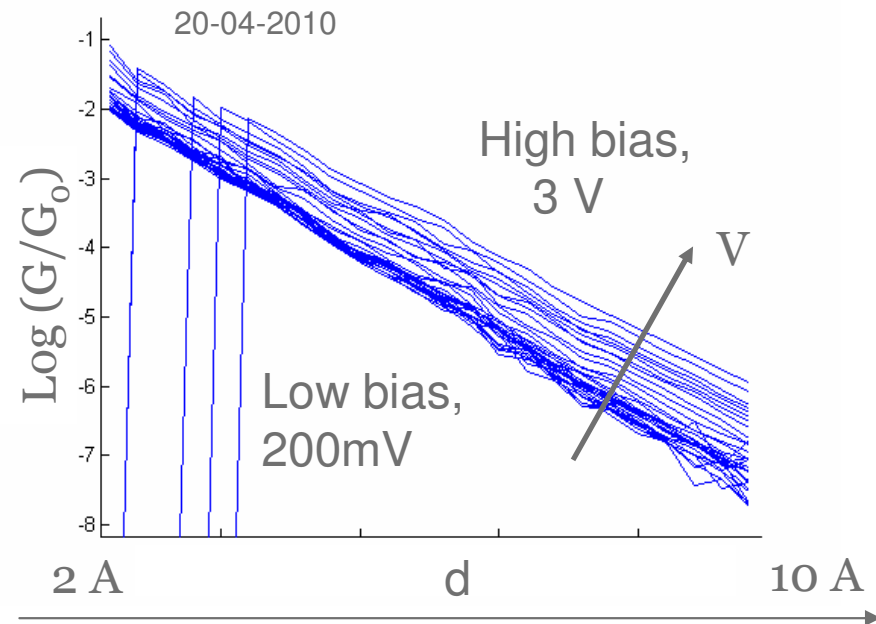
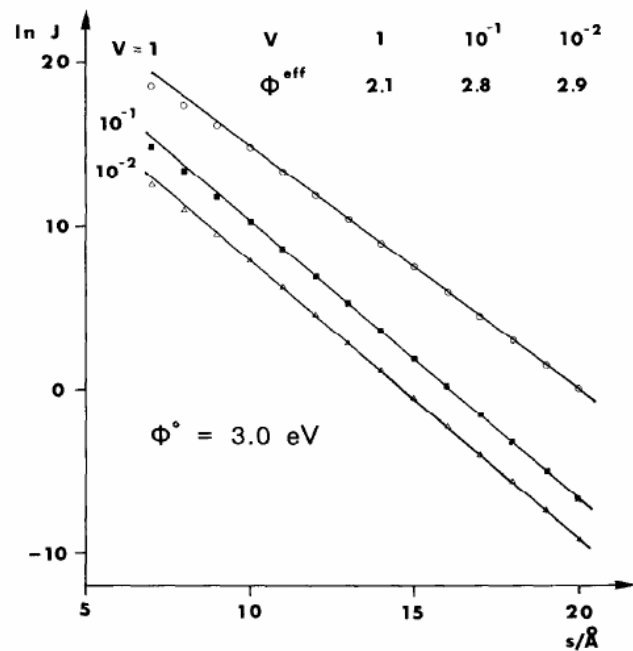


- Numerical derivative from a fit within 50 mV, average of bwd/fwd sweep
- logarithmic color scale of dI/dV in G_0 (-1=0.1 etc.)
- General trend: dI/dV increases at given d with V (as expected from tunneling)
- So far no apparent anomalies in the color pattern.

Christian Martin



dI/dV as a function of d



- The overall slope of $dI/dV(d)$ decreases with increasing bias voltage.
- Simmons: $\bar{\varphi} = (\varphi - eV/2)$.