

# Spin caloritronics with cold atoms

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European Research Council

# Spin caloritronics with (ferromagnetic) metals

- Understanding of: (NB:  $\sigma = (\sigma_{\uparrow\uparrow} + \sigma_{\downarrow\downarrow})/2$ )

$$\begin{pmatrix} j_{\uparrow} \\ j_{\downarrow} \\ j_{Q\uparrow} \\ j_{Q\downarrow} \end{pmatrix} = \begin{pmatrix} \sigma_{\uparrow\uparrow} & \sigma_{\uparrow\downarrow} & \sigma TS_{\uparrow\uparrow} & \sigma TS_{\uparrow\downarrow} \\ \sigma_{\downarrow\uparrow} & \sigma_{\downarrow\downarrow} & \sigma TS_{\downarrow\uparrow} & \sigma TS_{\downarrow\downarrow} \\ \sigma P_{\uparrow\uparrow} & \sigma P_{\uparrow\downarrow} & \kappa_{\uparrow\uparrow} & \kappa_{\uparrow\downarrow} \\ \sigma P_{\downarrow\uparrow} & \sigma P_{\downarrow\downarrow} & \kappa_{\downarrow\uparrow} & \kappa_{\downarrow\downarrow} \end{pmatrix} \begin{pmatrix} -\nabla\mu_{\uparrow} \\ -\nabla\mu_{\downarrow} \\ -\nabla T_{\uparrow} \\ -\nabla T_{\downarrow} \end{pmatrix}$$

+ magnetization  
dynamics  
+ applications

*(Spin) drag effects  
due to interactions*

# Spin caloritronics with cold atoms

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- Does it exist?
- What can we learn from it?
- What is it good for?

# Collaborators

Ph. D. Students: Ties Lucassen, Aaron Swaving, Hedwig van Driel, Erik van der Bijl, Martijn Mink,  
postdocs: Clement Wong, Alice Bezett  
Prof. Cristiane de Morais and  
Henk Stoof  
(*Utrecht University*)

Allan MacDonald (*UT Austin*)

Paul Haney (*NIST*)

Alvaro Núñez (*Valparaiso, Chile*)

Jairo Sinova (*Texas A&M*)

Achim Rosch's group (*Cologne*)

Christian Pfleiderers group (*TU Munich*)

R. Lavrijsen.+TU/e team

Giovanni Vignale (*Missouri*)

Marco Polini (*SNS Pisa*)

Acknowledgements:

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Maxim Mostovoy (*Groningen*)



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# First: introducing cold atoms

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# Introducing cold atoms (I)

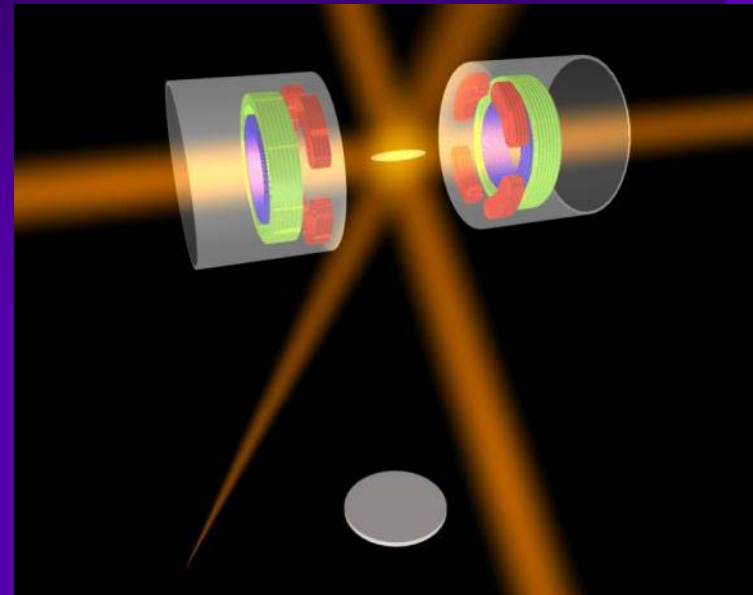
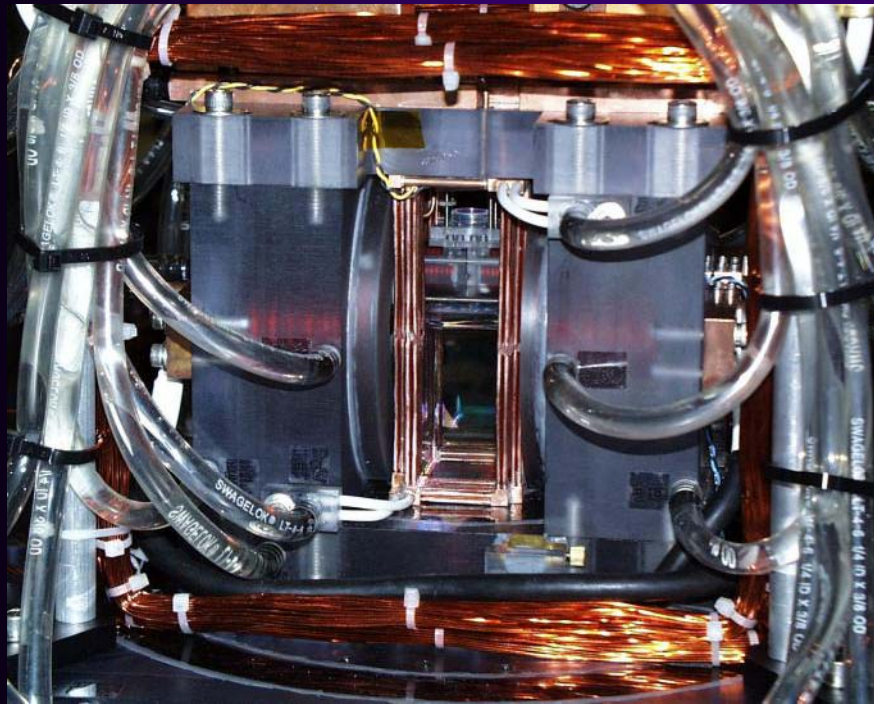
## Electrons in metals

- charge  $-e$
- Spin  $S=1/2$
- fermion
- ionic lattice
- disorder
- phonons
- spin-orbit coupling
- long range  $e-e$  interactions
- magnons (in ferromagnet)

## Trapped cold atoms

- neutral, e.g., Rb-87, Li-6/7, ...
- (hyperfine) spin  $F=...$
- Bosons and/or fermions
- magnetic and/or optical trap
- disorder *can be*
- phonons *engineered*
- spin-orbit coupling
- short-range atomic interactions
- magnons (in ferromagnet)

# Introducing cold atoms (II)



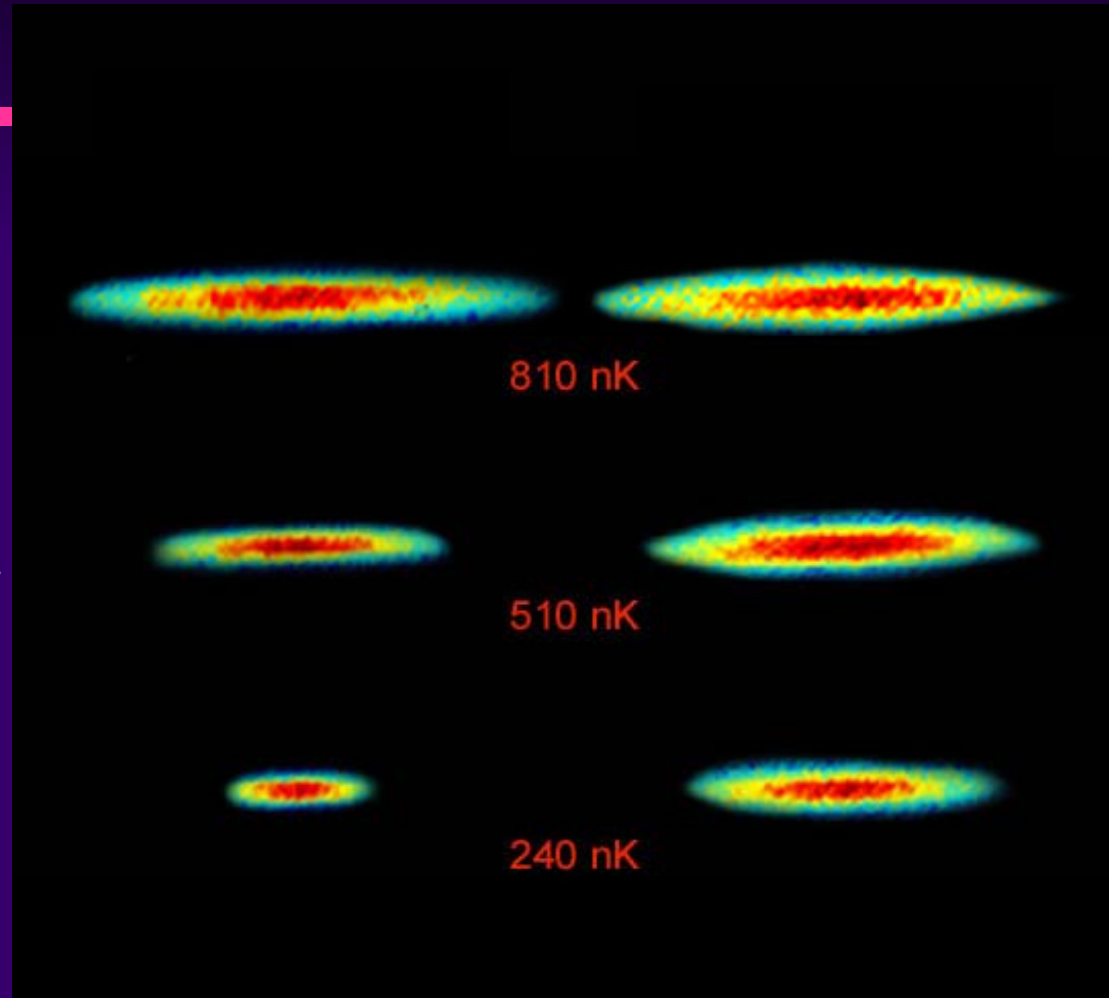
*Laser cooling, harmonic confining potential,  
evaporative cooling, absorption imaging*



# Introducing cold atoms (III)

*This experiment:  
few million atoms*

*(Generally ranges  
from  $10^4$ - $10^9$ )*



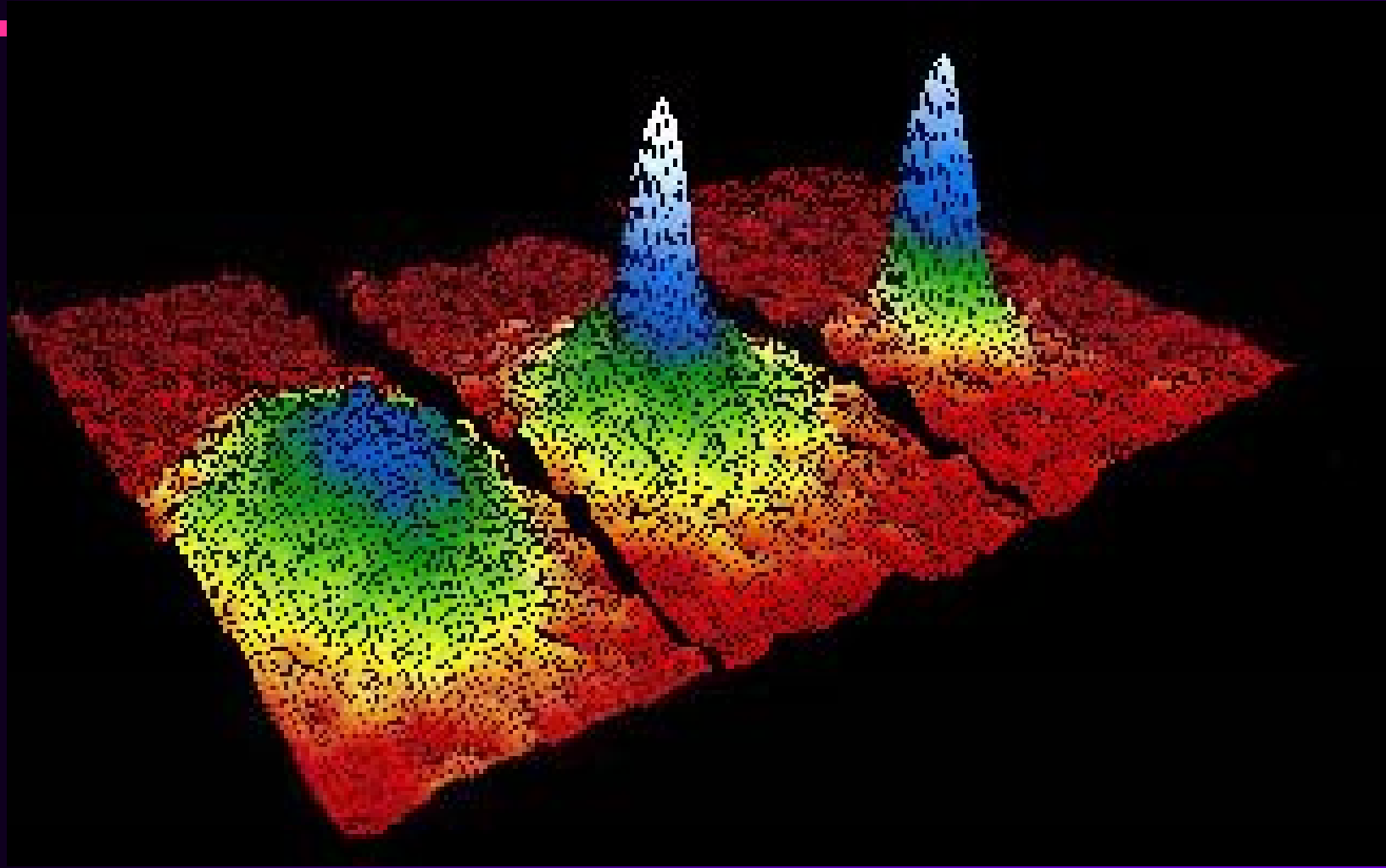
*Lithium-7*

*Lithium-6*

*(Boson -> Bose Condensation!)*

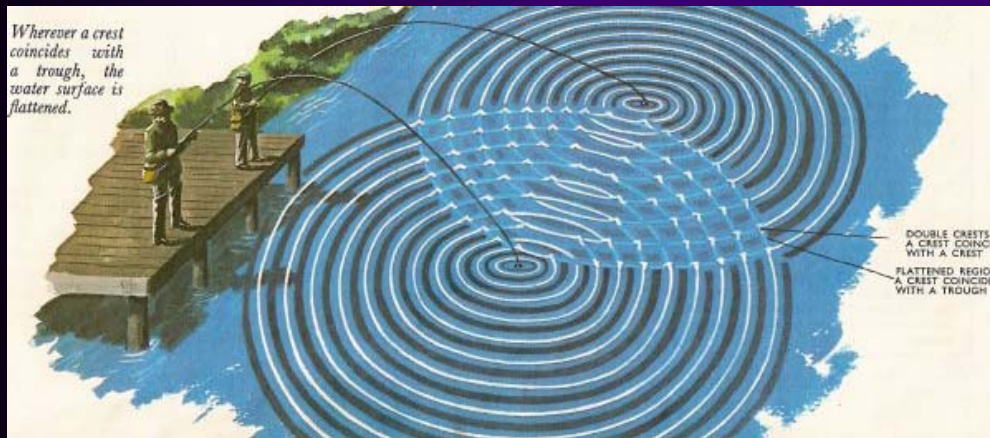
*(Fermion,  $T/T_F \sim 0.1$ )*

# First Bose condensate (1995)

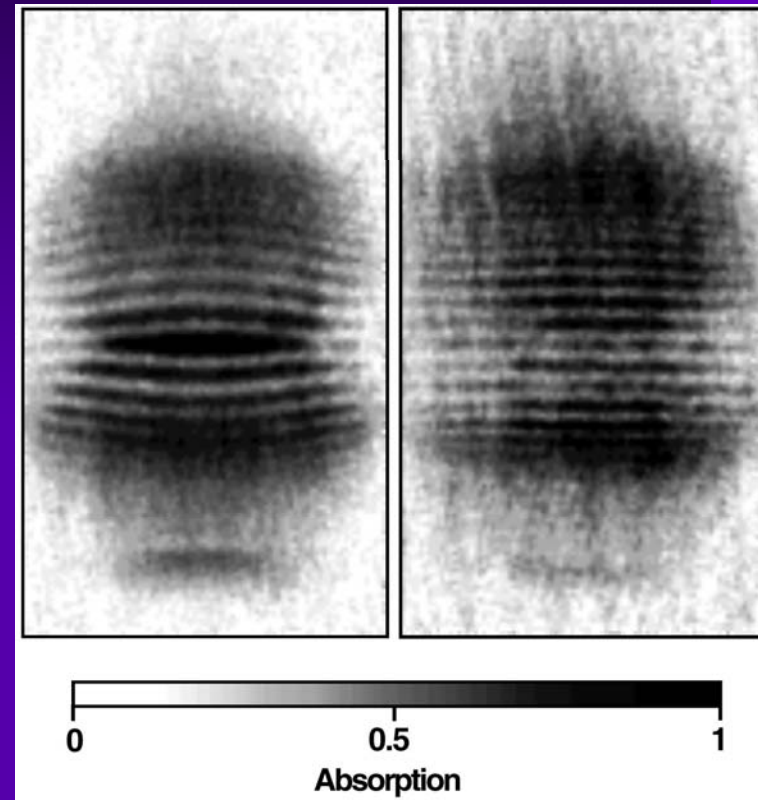


*C. Wieman, E. Cornell (Nobel prize, 2001)*

# Two interfering Bose condensates



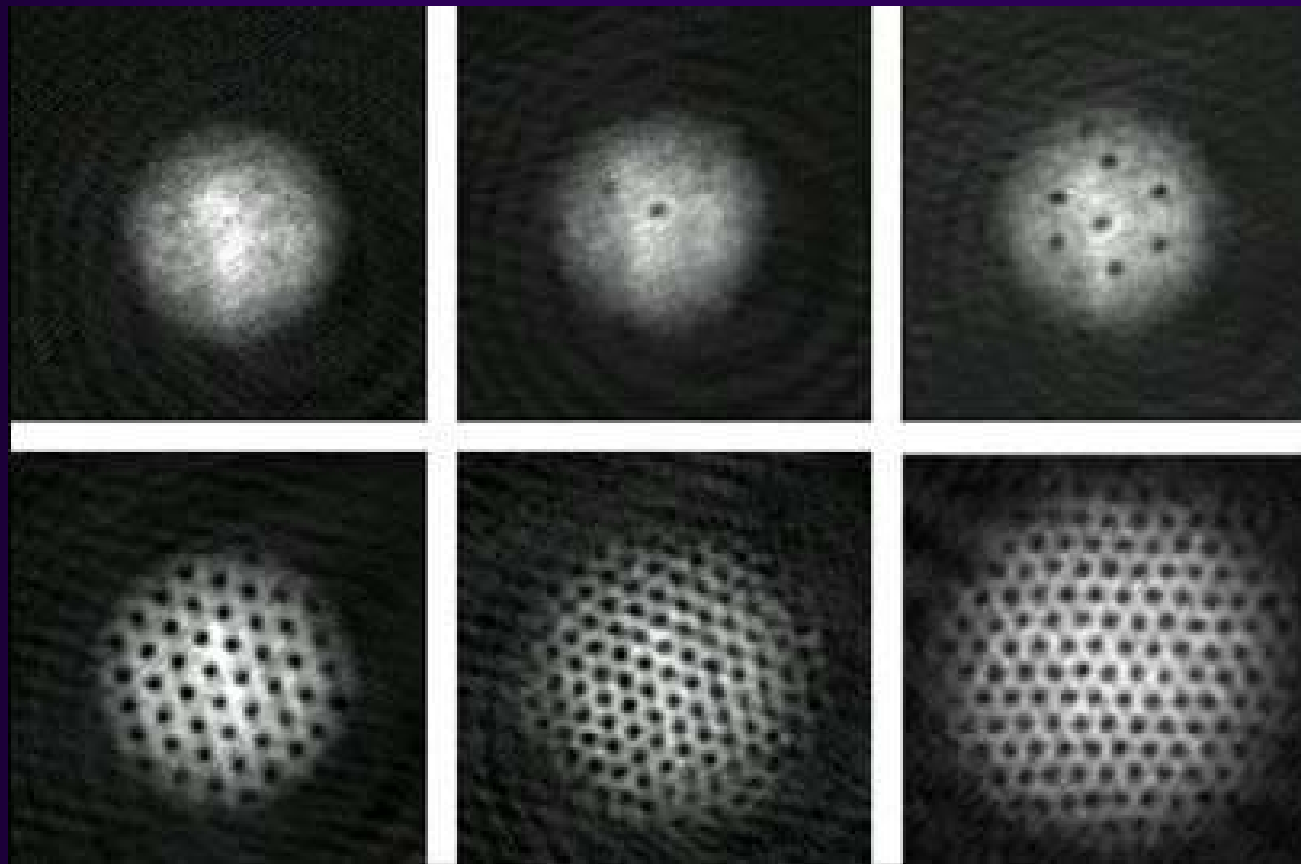
*Classical waves*



*“matter waves”*

*W. Ketterle (Nobel prize, 2001)*

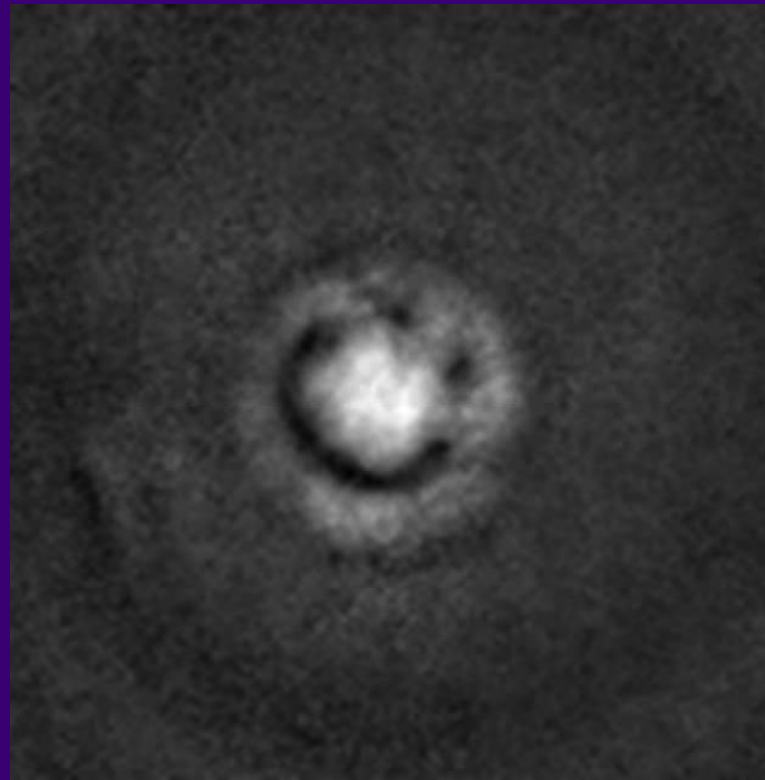
# Rotation: quantum vortices



*NB: rotation acts like magnetic field!!*

# Introducing cold atoms (IV)

- + many more (mostly equilibrium) results...e.g:



*happy Bose condensate*

# Spin caloritronics with cold atoms

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# Spin caloritronics with cold atoms? (I)



Cold atoms have spin (take for now  $F=1/2$ )

- Coupled mass (*not charge*), spin, and heat:

$$\begin{pmatrix} j_{\uparrow} \\ j_{\downarrow} \\ j_{Q\uparrow} \\ j_{Q\downarrow} \end{pmatrix} = \begin{pmatrix} \sigma_{\uparrow\uparrow} & \sigma_{\uparrow\downarrow} & \sigma TS_{\uparrow\uparrow} & \sigma TS_{\uparrow\downarrow} \\ \sigma_{\downarrow\uparrow} & \sigma_{\downarrow\downarrow} & \sigma TS_{\downarrow\uparrow} & \sigma TS_{\downarrow\downarrow} \\ \sigma P_{\uparrow\uparrow} & \sigma P_{\uparrow\downarrow} & \kappa_{\uparrow\uparrow} & \kappa_{\uparrow\downarrow} \\ \sigma P_{\downarrow\uparrow} & \sigma P_{\downarrow\downarrow} & \kappa_{\downarrow\uparrow} & \kappa_{\downarrow\downarrow} \end{pmatrix} \begin{pmatrix} -\nabla\mu_{\uparrow} \\ -\nabla\mu_{\downarrow} \\ -\nabla T_{\uparrow} \\ -\nabla T_{\downarrow} \end{pmatrix}$$

~~No~~ disorder, phonons, no relaxation of center-of-mass

$\sigma_{\uparrow\uparrow}, \sigma_{\downarrow\downarrow}, \sigma \rightarrow \infty$  but  $\sigma_{\uparrow\downarrow} = \sigma_{\downarrow\uparrow}$  affected by interactions

# Spin caloritronics with cold atoms? (II)

- System only reaches transport-steady-state

if:  $F_{\uparrow} = -F_{\downarrow} \equiv F_s$  and  $\nabla T_{\uparrow} = -\nabla T_{\downarrow} \equiv \nabla T_s$



Coupled spin and spin-dependent heat transport:

$$\begin{pmatrix} j_{\uparrow} - j_{\downarrow} \\ j_{Q\uparrow} - j_{Q\downarrow} \end{pmatrix} = \begin{pmatrix} j_s \\ j_{Qs} \end{pmatrix} = \begin{pmatrix} \sigma_s & \sigma_s T S_s \\ \sigma_s P_s & \kappa_s \end{pmatrix} \begin{pmatrix} F_s \\ -\nabla T_s \end{pmatrix}$$



Can bulk transport regime be reached?

electrons:  $\tau \sim \text{ps}$ ,  $l \ll L$  (typically), cold

atoms,  $\tau \sim \text{ms}$ ,  $l > L$ , or  $l < L$



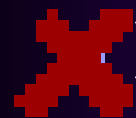
# Spin caloritronics with cold atoms? (III)

- Study of:

$$\begin{pmatrix} j_{\uparrow} - j_{\downarrow} \\ j_{Q\uparrow} - j_{Q\downarrow} \end{pmatrix} = \begin{pmatrix} j_s \\ j_{Qs} \end{pmatrix} = \begin{pmatrix} \sigma_s & \sigma_s T S_s \\ \sigma_s P_s & \kappa_s \end{pmatrix} \begin{pmatrix} F_s \\ -\nabla T_s \end{pmatrix}$$



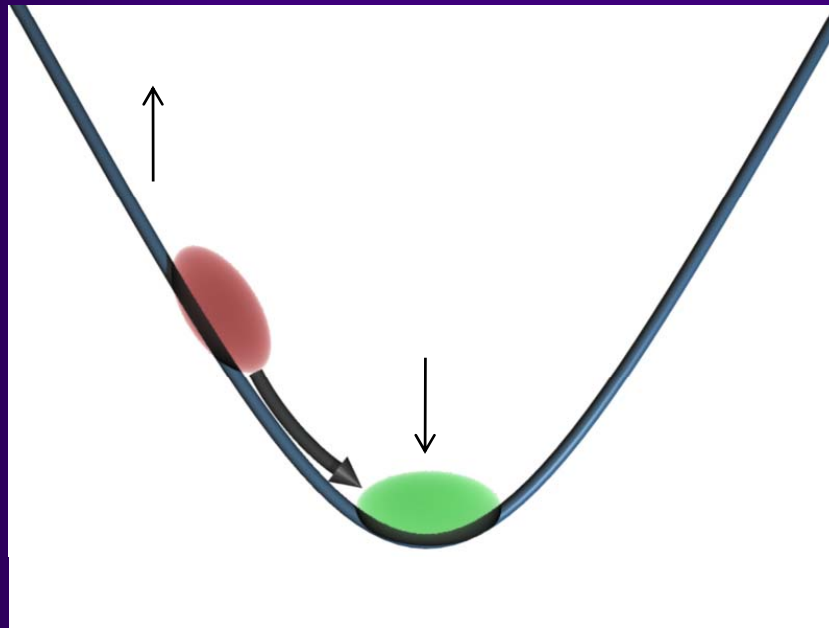
(Theory of)...spin caloritronics w/ cold atoms!



Experiment? (no leads, V/I meters, ...)

# Example: measuring spin conductivity

$$j_s = \sigma_s F_s; \text{ define: } \sigma_s = \frac{n\tau_{sd}}{m} \quad \text{“Spin drag”}$$



*Damping rate of spin-dipole model =  $1/\tau_{sd}$*

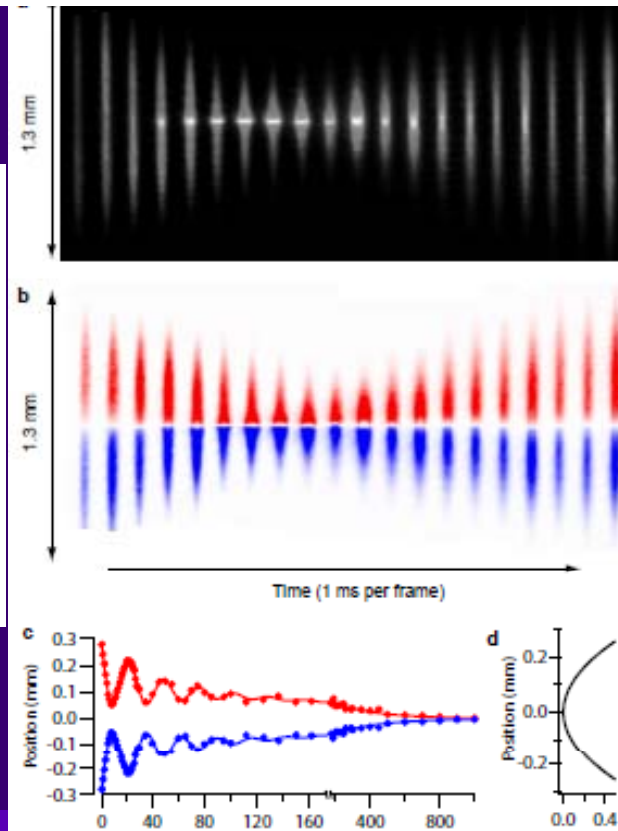
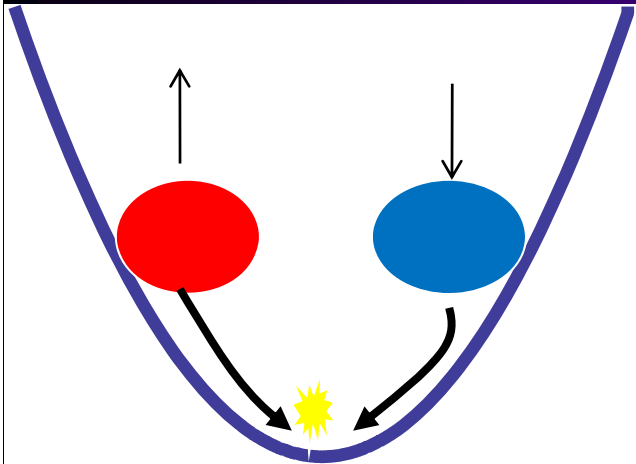
# Experiments on cold fermions

LETTER

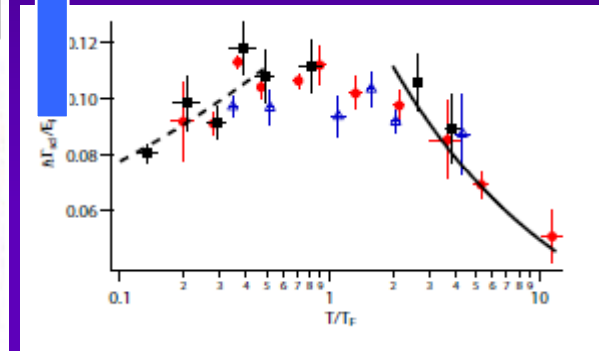
doi:10.1038/nature09989

## Universal spin transport in a strongly interacting Fermi gas

Ariel Sommer<sup>1,2,3</sup>, Mark Ku<sup>1,2,3</sup>, Giacomo Roati<sup>4,5</sup> & Martin W. Zwierlein<sup>1,2,3</sup>



$1/\tau_{sd}$



temperature

Ongoing experiments with bosons: P. van der Straten (Utrecht)

# Theory of spin resistivity of cold gases:

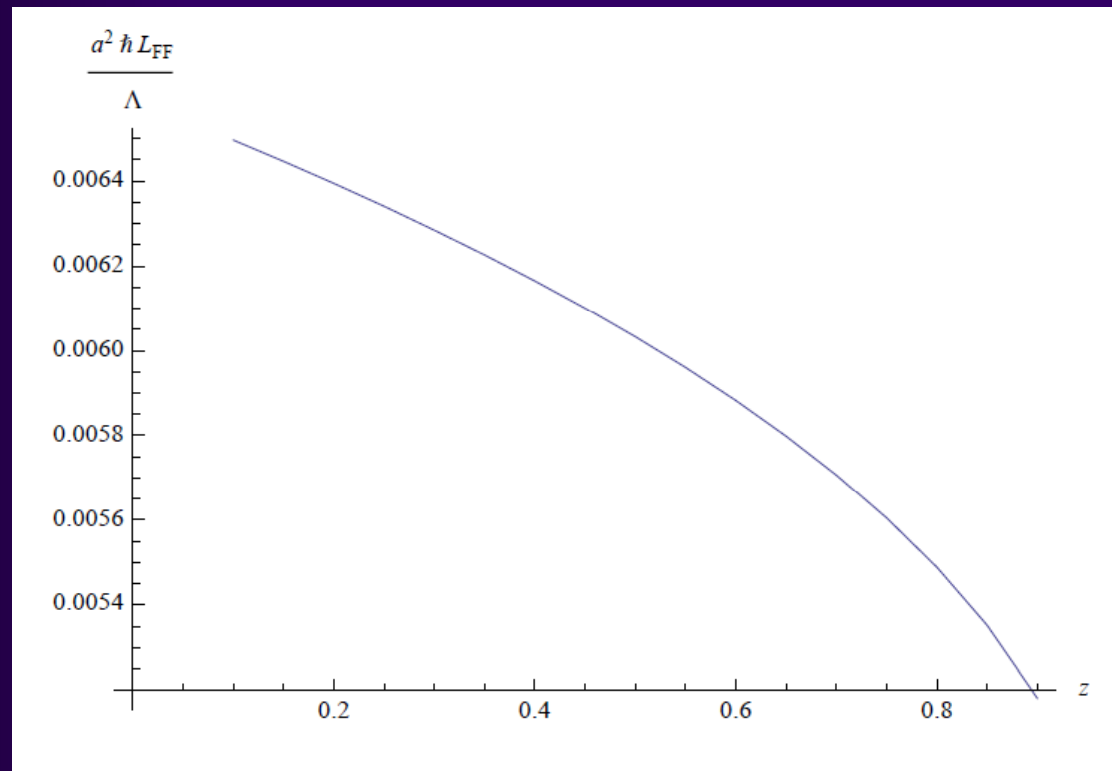
$$\rho_s \sim \frac{1}{\tau_{sd}} \sim T^2 \quad (\text{fermions "blocking" in 3D}) \quad 10^{-9} \text{ } \Omega\text{m}$$

$$\rho_s \sim \frac{1}{\tau_{sd}} \sim T^{-2} \quad (\text{bosons "lasing" in quasi-1D}) \quad 10^{-5} \text{ } \Omega\text{m (use charge}=e)$$

Enhancement of spin resistivity  
(reduction of spin conductivity)  
upon approaching  
critical temperature for Bose condensation!  
-> interesting temperature dependence  
in all transport coefficients?

# Some more (very preliminary theory results) for bosons (I):

“Spin conductivity”



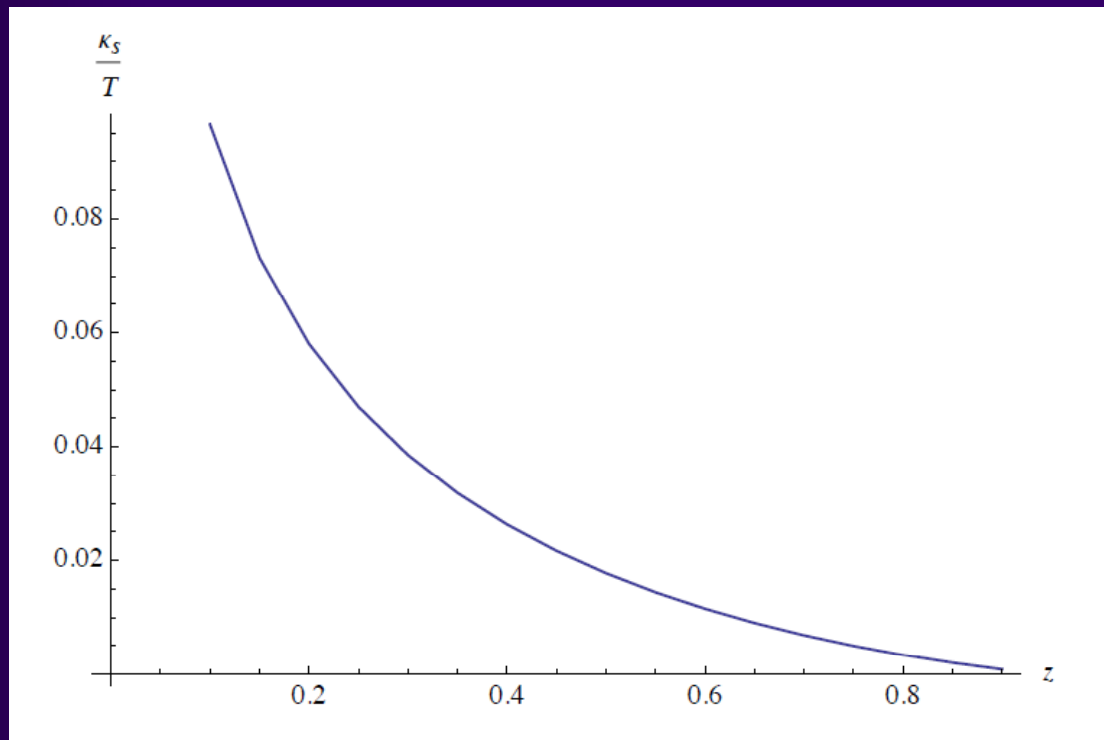
*high T*

$T_{BEC}$

*low T*

# Some more (very preliminary theory results) for bosons (II):

“spin-dependent heat conductivity”



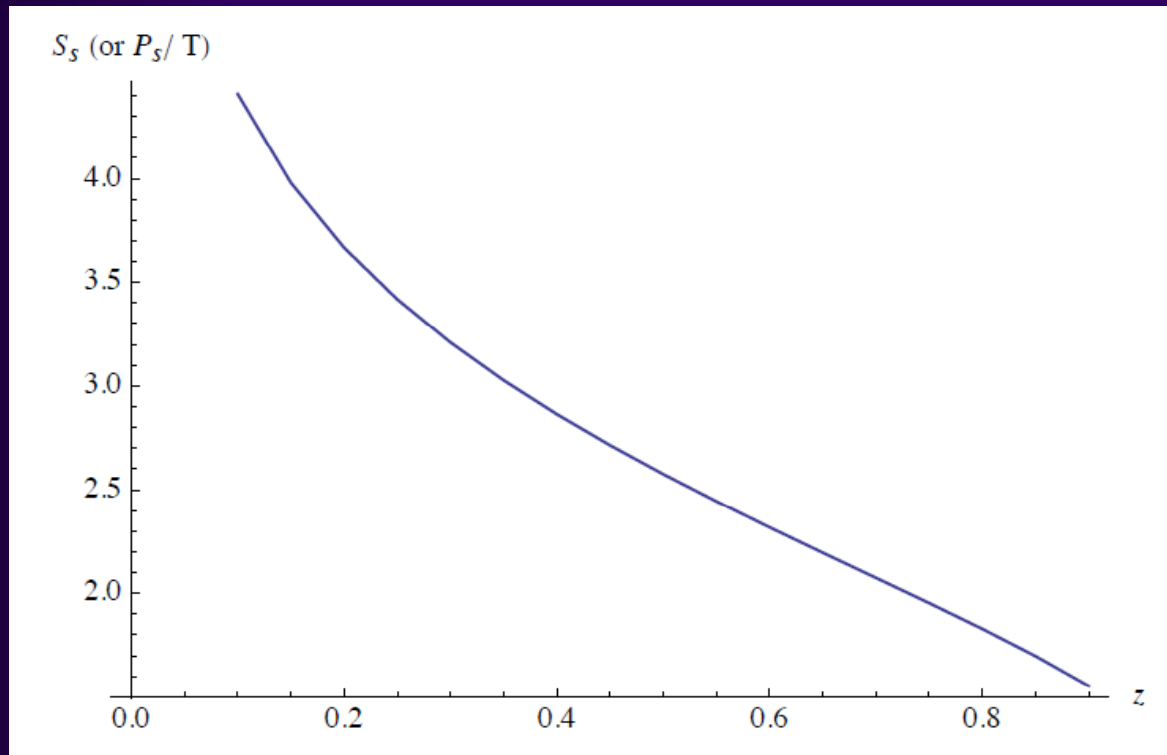
*high T*

$T_{BEC}$

*low T*

# Some more (very preliminary theory results) for bosons (III):

“Seebeck/Peltier”



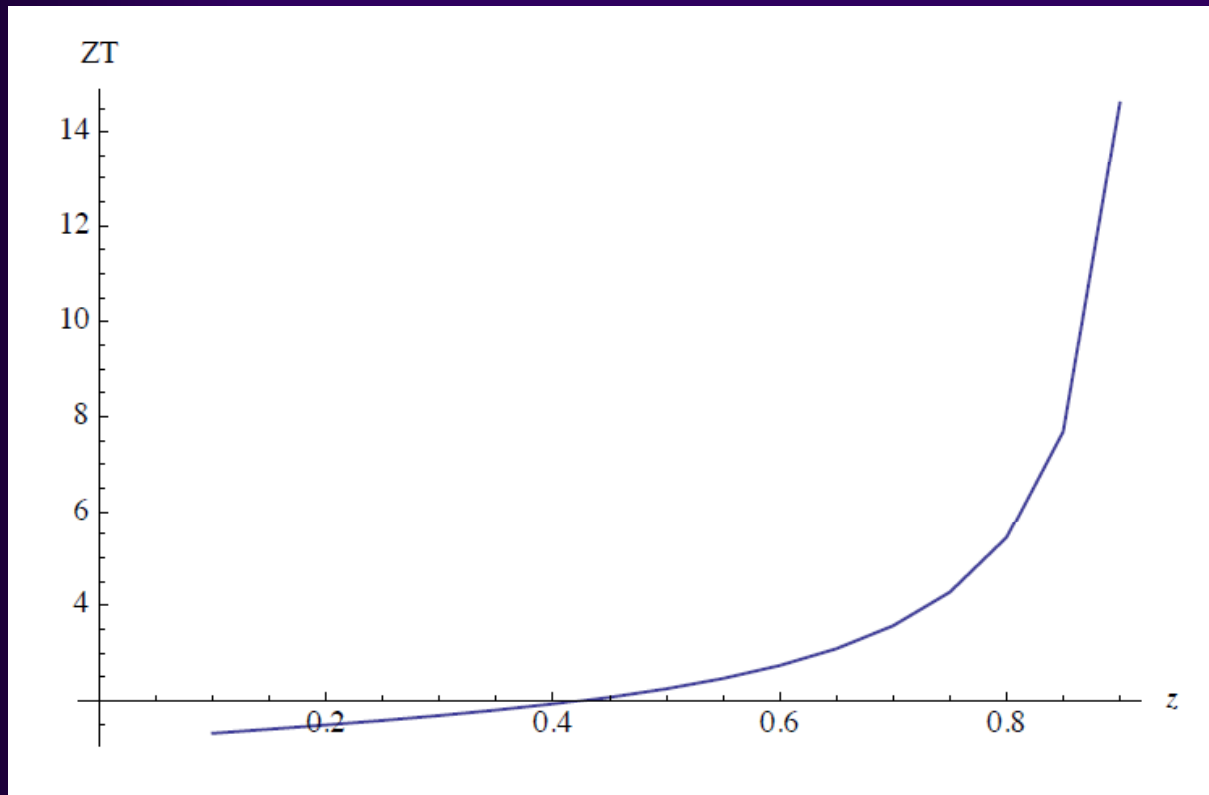
*high T*

$T_{BEC}$

*low T*

# Some more (very preliminary theory results) for bosons (IV):

“Figure of merit”



*high T*

$T_{BEC}$

*low T*



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Does it exist?

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# Spin caloritronics with cold atoms

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Does it exist?

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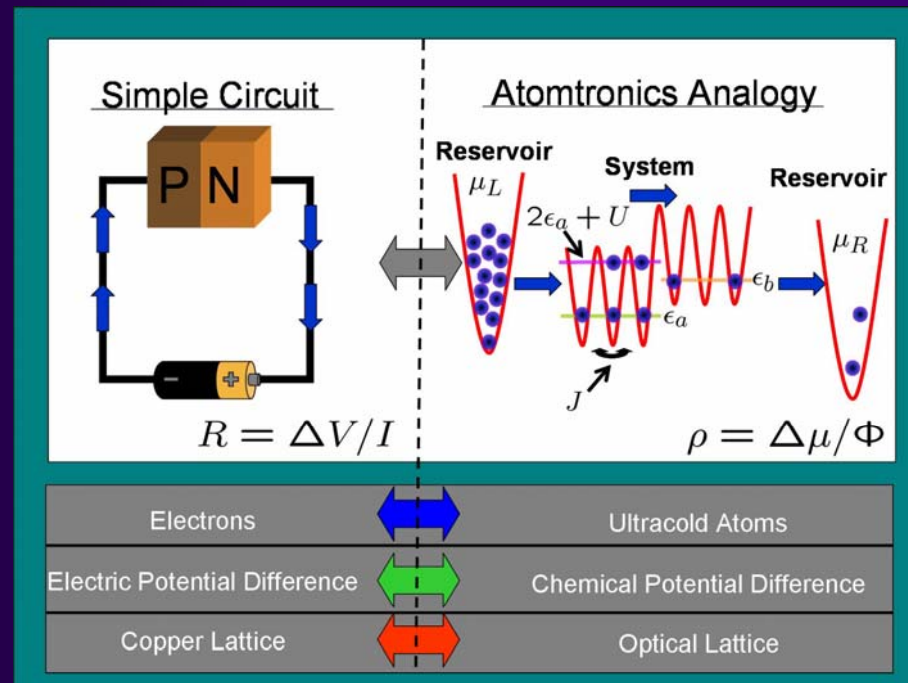
# What can we learn from it and what is it good for?

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- Intrinsically interesting fundamental physics
- Cold atom systems are easy and tunable -> simulate models, solve controversies, etc... (Hubbard model, high T-c)
- New regimes (e.g. spin drag effects)
- Magnonic (bosons) spintronics; Bose condensation of magnons
- Direct applications?

# Atomtronics?

- Direct applications of cold-atom systems:



*Murray Holland,  
Dana Anderson*

- Probably not consumer electronics,  
quantum computing?

# Spin caloritronics with cold atoms

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Does it exist?

- What can we learn from it and what is it good for?

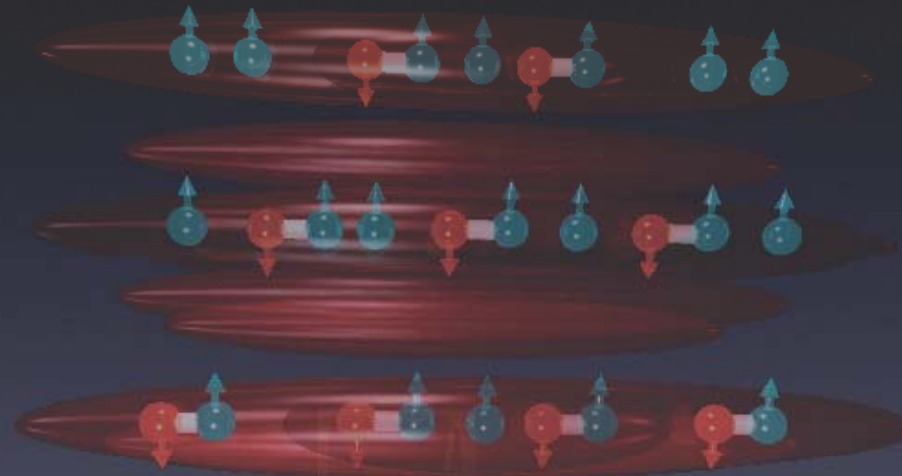
# NEWSPIN<sup>2</sup>

## Spin physics and topological effects in cold atoms, condensed matter, and beyond

International Winter School and Workshop

December 12<sup>th</sup>-17<sup>th</sup> 2011

Mitchell Institute of Fundamental Physics  
College Station, Texas



### Topics

- Magnetism in cold atoms
- Spin and Anomalous Hall effect
- Spin transfer and spin pumping
- Spin motive forces
- Controlling spins by light
- Spin orbit coupling in cold-atom systems
- Spin-imbalance in cold Fermi gases
- Topological insulators
- Dirac physics in cold atoms and condensed matter
- Pseudospin physics

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